

On the convergence of a new iterative algorithm of three infinite families of generalized nonexpansive multi-valued mappings

DHIRENDRA BAHUGUNA and ANUPAM SHARMA*

Department of Mathematics and Statistics, Indian Institute of Technology Kanpur, Kanpur 208 016, India *Corresponding author. E-mail: dhiren@iitk.ac.in; anupam@iitk.ac.in

MS received 10 August 2016; revised 11 January 2017; accepted 19 January 2017; published online 30 July 2018

Abstract. In this paper, we establish some weak and strong convergence theorems for a new iterative algorithm under some suitable conditions to approximate the common fixed point of three infinite families of multi-valued generalized nonexpansive mappings in a uniformly convex Banach spaces. Our results generalize and improve several previously known results of the existing literature.

Keywords. Common fixed point; generalized nonexpansive map; three step iterative scheme; weak and strong convergence; condition (A').

2010 Mathematics Subject Classification. 54H25, 47H09, 47H10.

1. Introduction

In recent years, approximation of fixed point of multi-valued nonexpansive mappings and multi-valued generalized nonexpansive mappings by iteration has been studied by many authors (see [2,3,20,22,24,26,28,31,32]). The fixed point theory of multi-valued mappings is much more complicated and difficult than the corresponding theory of singlevalued mappings and has many fruitful applications in various fields, for example, game theory and mathematical economics. Thus, it is natural to extend the known fixed point results for single-valued mappings to the setting of multi-valued mappings. However, some classical fixed point theorems for single-valued nonexpansive mappings have already been extended to multi-valued mappings. The first set of results in this direction were established by Markin [17] in Hilbert spaces and by Browder [4] for spaces having weakly continuous duality mapping. Dozo [10] generalized these results in a Banach space satisfying Opial's condition.

In 1969, Nadler [18] proved a fixed point theorem for multi-valued contraction mappings and convergence of a sequence and also extended theorems on the stability of fixed points of single-valued mappings. Markin [17] first used the Hausdorff metric to study the fixed points for multi-valued contractions and nonexpansive mappings. Later in 1997, Hu *et al.* [13] obtained common fixed point of two nonexpansive multi-valued mappings satisfying certain contractive conditions.