

# Working Stress Versus Limit State Method-A Gistical View For Designing of Rcc Stuctures

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## ABSTRACT

The title of this technical paper deals and demonstrates the pros and cons of WSM versus LSM and highlights the revised code of design of RCC structures as LSM. LSM is better and revised method over working stress and LSM is in vogue .Though in LSM permissible stresses are more than WSM & designed load is multiplied with factor 1.5, even the size of section remains small and steel remains more, even than the cost remains less than WSM. The differentiation must be known by elite readers for getting known the changing procedure of design of RCC structures using both methods.

**Key Words:-**LSM-Limit State Method, WSM-Working State Method, RCC-Reinforced Cement Concrete, fck-Charateristic Strength of Concrete, cbc-Permissible Compressive Stress of Concrete in Bending etc.

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## INTRODUCTION

While designing RCC structures like beam, slab, column, portal frame, retaining wall, dam, chimneys, over-head water tanks, bunkers, stair-case and silos etc., it has been observed that out of three methods of designing only two methods are popular and in vogue.

In existing scenario or a decade back only, limit state method has been emphasized and put into the syllabus of civil engineering whether it is in diploma or degree. The past method working stress, was full of easy conceptual basis and mend for mild steel having grade Fe-250, where the hooks are provided at ends of bar, so that the bond between the cement concrete and steel surface could be perfect and no slip could be possible and load of tensile be transferred on steel and compression on concrete, as concrete is better in compression while steel is in tension alike in compression. The steel is now used as HYSD bars or TOR steel bars and have more yield strength like Fe-415, Fe-500, and Fe-550, whose surface has corrugations and due to this the concrete makes better bond with steel surface. By this reason the bars have bends at ends rather than hooks.

Also the grade of cement concrete has been increased from M-15 to M-20, M-25 and M-30 for general and specified works. Similarly the design procedure has been modified and treated as limit state method.

The below paragraph/sub title, demonstrates the actual differentiation in theoretical aspect, materials grade, permissible strength, changing designing concept, checking concept and respective formulas etc.

## DIFFERENTIAL ASPECT

Since the method of limit state has been in prevailing and commonly in use, hence pros over working stress are being emphasized below in two segments viz first part as working stress and limit state as second part.

Working stress method is based on theoretical aspect and has easy calculation.

Working Stress	Limit State
(1) Some assumptions are followed up for making simple calculation.	(1) Some assumptions are followed up for making up simple calculation.
(2) Permissible stress of concrete in bending is taken $f_{ck}/3$ , here $f_{ck}$ =characteristic strength of concrete like M-15,M-20,M-25,M-30,M-35 & M-40 respectively has $f_{ck}$ 15,20,25,30,35 & 40 N/square mm. So permissible stress of concrete in bending respectively becomes 5, 7, 8.5, 10, 11.5 and 13.	(2) Permissible stress in concrete = <b>0.446<math>f_{ck}</math></b> For M10,15,20,25,30,35 and 40 Stress in concrete =4.46, 6.69, 8.92, 11.15, 13.38, 15.61 and 17.84 N/sq mm respectively.
(3) Permissible stress of steel in tension is taken $f_y/1.78$ , here $f_y$ =yield strength of steel, where $f_y$ is 250 N/sq. mm, stands Fe-250 grade steel. So permissible stress of steel for $f_y$ -250 is 140 N/sq.mm. For Fe-350/415/500/550 the values may be 190/230/275/300 N per sq.mm.	(3) Permissible stress in steel = <b>0.87<math>f_y</math></b> For Fe-250,350,415,500 & 550, the respective permissible stress =217.5,304.5,361,435 & 478.5 N/sq.mm.
(4) Permissible direct stress of concrete in compression is taken $f_{ck}/4$ , where for $f_{ck}$ values 15, 20, 25, 30, 35 & 40, direct stress respectively taken 2.5,4,5,6,8,9 & 10 N per sq. mm.	(4) Permissible direct stress of concrete in compression = <b>0.4<math>f_{ck}</math></b> . For M10,15,20,25,30,35 & 40 ,respective stress will be 4,6,8,10,12,14 & 16 N/sq.mm.
(5) Permissible stress of steel in compression $f_{sc}$ ,is taken 130,130,190 & 190 N per sq.mm, respectively for Fe-250,350,415 & 500 grade steel.	(5) Permissible stress of steel in compression = <b>0.67 <math>f_y</math></b> For Fe250, 350, 415,500 & 550, the respective permissible stress of steel in compression =167.5, 234.5, 278, 335 & 368.5 N/ sq. mm.
(5A) Modular ratio $m$ is taken $E_s/E_c$ =modulus of elasticity for steel/modulus of elasticity for concrete or $280/3$ multiplied by permissible stress of concrete in bending. Hence $m=18, 13,11,9,8$ & $7$ for respective grade of concrete 15,20,25,30 & 40.	(5A) No modular ratio $m$ is taken into account.
(6) $C$ =compressive Force of Concrete $T$ =Tensile Force by Steel	(6) $C_u$ =compressive Force of concrete. $T_u$ = Tensile Force of steel
(7) Lever Arm $Z_a$ =Actual lever Arm= $(d-X_a/3)$ $Z_c$ =Critical Lever Arm= $d-X_c/3$	(7) Lever Arm Actual lever arm $Z=(d-0.42X_u)$ Critical Lever Arm $Z_{max}=d-0.42x_{max}$
(8) Critical neutral axis = $X_c$ (m)(Permissible stress of concrete in bending). $d/(m)$ (permissible stress of concrete in bending) +permissible stress of steel in tension. (For $m=18, M-15, Fe-250, X_c=0.39d$ ) ( $m=18, M-15, Fe-350, X_c=0.32d$ ) ( $m=18, M-15, Fe-415, X_c=0.28d$ ) ( $m=18, M-15, Fe-500, X_c=0.246d$ )	(8) Critical Neutral Axis $X_{umax}$ $[0.0036/X_{umax}] = [(0.87f_y/E_s)+0.002]/(d-X_{umax})$ $E_s=200000\text{N/sq.mm}$ $X_{umax}=(700)(d)/(1100+0.87f_y)$ (For M15 & Fe250, $X_{umax}=0.53d$ ) (For M15 & Fe 350, $X_{umax}=0.51d$ ) (For Fe 415, $X_{umax}=0.48d$ )
(9) Stress Diagram in compression zone Triangular $c_b c, X_a, d-X_a, st/m, T, C, X_a/3, Z_a$ . Here $c_b$ =permissible bending stress of concrete in	(Fe 500, $X_{umax}=0.46d$ )  (9) Stress diagram in compression zone Rectangular and parabolic $0.446f_{ck}, 3X_u/7, 4X_u/7, 0.42X_u,$

<p>bending Xa=Actual Neutral Axis, T=total tensile force, C=total compressive force</p> <hr/> <p>(10)-Compressive force in balance condition Xa=Xc C=b×Xc×cbc/2</p> <hr/> <p>11-Tensile force=T=steel area×stress T=Ast×st</p> <hr/> <p>12-Actual Neutral Axis =Xa Xa=area moment of compression zone with respect to neutral axis=equivalent concrete area moment in tension zone with respect to Neutral axis against tensile steel <math>b \times X_a \times X_a / 2 = m \times A_{st}(d - X_a)</math></p> <hr/> <p>13-Permissible position of Xa and Xc Xa&lt;Xc=under reinforced Means less provided steel as per requirement and by this cause steel will fail before collapse. Xa=Xc=balance section Means steel provided is same as required, by this cause both will fail simultaneously. Xa&gt;Xc=over reinforced , Means provided steel is more than required, hence concrete will fail before the steel.</p> <hr/> <p>(14)-Percentage of steel ,P%=Ast×100/b.d</p> <hr/> <p>(15)-Permissible steel ... For M-15 and Fe-350 p% steel=50×X1xcbc/st 0.42% For M25,Fe-415, p%=0.53% For M30,Fe-415,p%=0.61% Less steel than Limit State</p> <hr/> <p>16-Critical Lever Arm Z=(d-Xc/3) =(d-0.33Xc) For M-15 &amp; Fe-250,Xc=0.39d, Z=0.87d For M-15 &amp; Fe-350, Xc=0.32d,Z=0.89d For M-15 &amp; Fe-415,Xc=0.28d, Z=0.90d</p> <hr/> <p>17-Moment of resistance (A) Xa&lt;Xc= under reinforced Moment =M=M steel=Tensile force ×Z M=(Ast×st)(d-Xa/3) (B)Xa=Xc=balance section M steel=Ast×st(d-Xa/3) Or M concrete =b×Xa×cbc(d-Xa/3)/2 (C)Xa&gt;Xc=over reinforced Concrete will fail. M concrete =b×Xa×cbc(d-Xa/3)</p> <hr/> <p>(18)Moment Resistance Factor Q=0.5×cbc ×X1×Z1×b×d×d</p>	<p>Tu=total tensile force, Cu=total compressive force.</p> <hr/> <p>(10)Compressive force in balance condition Xu=Xumax Cu=0.36fck.Xu.b</p> <hr/> <p>(11)Tensile Force Tu=0.87fy.Ast</p> <hr/> <p>(12)For actual neutral Axis Cu=Tu 0.36fck.Xu.b =0.87fy.Ast <b>Xu=0.87fy.Ast/0.36fck.b</b> Xu=2.416 fy.Ast/fck.b</p> <hr/> <p>(13) Permissible position of Xu and Xumax. Xu&lt;Xumax =under reinforced Means less provided steel as per requirement and by this cause steel will fail before collapse. Xu=Xumax =balance Means steel provided is same as required, by this cause both will fail simultaneously. Xu&gt;Xumax =over reinforced =not desired</p> <hr/> <p>(14)Percentage steel p%=Ast×100/b.d</p> <hr/> <p>(15)For Permissible Steel Cumax=Tumax 0.36.fck.Xumax.b=0.87fy.Ast p% steel=41.4.Xumax.fck/fy. d (For M15, Fe-350,p% steel =0.88%) For M25, Fe-415,p% steel=1.2% For M30,Fe-415,p%=1.44% More steel than Working Stress</p> <hr/> <p>(16)Critical Lever Arm Z=(d-0.42Xumax) For M15,Fe250,Z=0.78d For M15,Fe350,Z=0.79d For M15,Fe415,Z=0.80d</p> <hr/> <p>(17)-Bending Moment Condition <b>(A)Xu&lt; Xumax =Under Reinforced</b> ,Steel will fail earlier. Moment Mu steel=Tu× lever arm Mu steel=0.87fy.Ast(d-0.42Xu) <b>(B)Xu=Xumax =balance</b> Mu=0.36fck.Xumax.b(d-0.42Xumax) <b>(C)Xu&gt;Xumax =over reinforced =not desired in limit state.</b> Mu=Mumax =0.36fck.Xumax.b(d-0.42Xumax)</p>
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<p>cbc=permissible compressive stress of concrete in bending  <math>X_1</math>=Coefficient of neutral Axis,<math>Z_1</math>=Coefficient of lever Arm.          For M-15 &amp; Fe-250,  <b><math>Q=0.5 \times 5 \times 0.39 \times 0.87 = 0.85 \text{ N/sq.mm.}</math></b></p> <hr/> <p>(19)Designed Load          Designed load=Incoming Load          If incoming load=50 KN/m then          Designed load=50KN/m...</p> <hr/> <p>[(20)Nominal Shear stress or incoming Shear Stress  <math>t_v = V/b.d</math>  <math>V</math>=maximum shear force  <math>b.d</math>= shear area</p> <hr/> <p>(22)Shear Force borne by bent-up bar  <math>V_b = A_{sv} \times s_v \times \sin 45^\circ</math>  <math>= 0.707 \times A_{sv} \times s_v</math>          Here <math>s_v</math>=permissible tensile or shear stress similar to <math>t_s</math>  <math>A_{sv}</math>=area of bent-up bar</p> <hr/> <p>(23)Shear Force borne by Stirrups  <math>V_s = A_{sv} \times s_v (d/s)</math> Or <math>S = A_{sv} \times s_v \times d / V_s</math>          Here <math>S</math>=spacing  <math>d</math>=effective depth of beam  <math>A_{sv}</math>=area of two leg stirrup.</p> <hr/> <p>(24)Shear Force borne by Concrete  <math>t_c</math>=permissible bond stress of concrete, dependent on %age steel of straight bar at end bottom and concrete grade.          This can be taken from tables by Interpolation.          %age steel =0.15% or less, <math>t_c=0.18, 0.18, 0.19</math> for M15,20,25 respectively.          %age steel =0.25%,<math>t_c=0.22, 0.22, 0.23</math>          %age steel =0.50%,<math>t_c=0.29, 0.30, 0.31</math></p> <hr/> <p>(25)Shear Strength of concrete for Slab          The value of <math>K</math> is multiplied by <math>t_c</math> for slab.  <math>K</math>=coefficient dependent on slab thickness.          Slab depth=150mm or less,175mm,200mm, 225mm, 250mm, 275mm,300mm or more.  <math>K=1.3, 1.25, 1.20, 1.15, 1.10, 1.05, 1.00</math> respectively.</p> <hr/> <p>(26)Maximum Shear Stress borne by Concrete  <math>t_c</math> maximum = dependent on concrete grade.  <math>t_c</math> maximum =1.6,1.8,1.9,2.2,2.3,2.5 for beam under respective grade of concrete M-15,20,25,30,35,40.  <math>t_c</math> maximum =0.8,0.9,0.95,1.1,1.15,1.25 for slab under concrete grade15,20,25,30,35,40.</p> <hr/> <p>(28)<math>t_v &gt; t_c</math> maximum =need to change the design.</p> <hr/> <p>(29)Design for Shear Reinforcement.          (A)<math>t_v &lt; t_c / 2</math>=No shear arrangement required</p>	<p>-----          (18)Moment Resisting Factor  <math>X_u = X_{u \max}</math>  <math>\mu_{\text{limit}} = \mu_{c \max} \times Z</math>          (For M15,Fe250,<math>X_{u \max} = 0.53d</math>)  <math>\mu_{\text{limit}} = 0.149 f_{ck} . b . d . d</math>  <b><math>Q_u = 0.149 \times 15 = 2.235 \text{ N/sq.mm for M15.}</math></b></p> <hr/> <p>(19)Designed Load or Factored Load          Designed load=<math>1.5 \times</math>Incoming Load          If incoming load=50KN/m, Designed load=75KN/m          Factored moment=<math>1.5 \times</math>Given Moment          Factored Shear =<math>V_u = 1.5 \times</math>Given Shear</p> <hr/> <p>(20) Nominal Shear stress or incoming Shear Stress  <math>t_{uv} = V_u / b.d</math>  <math>V_u</math>=maximum factored shear force</p> <hr/> <p>(22)Shear Force borne by bent-up bar  <math>V_{ub} = A_{sv} \times s_v \times \sin 45^\circ</math>  <math>= 0.707 \times A_{sv} \times 0.87 f_y = 0.757 \times A_{sv} \times f_y</math>          Here <math>A_{sv}</math>=total cross sectional area of bent-up bars.</p> <hr/> <p>(23)Shear force borne by stirrups  <math>V_{us} = A_{sv} \times s_v (d/s)</math> Or Spacing <math>s = A_{sv} \times s_v \times d / V_{us}</math>          Here <math>s</math>=spacing of stirrups. <math>s_v = 0.87 f_y</math>,  <math>A_{sv}</math>=cross sectional area of stirrup.          For 8mm size two leg stirrups <math>A_{sv} = 2 \times 50 = 100 \text{ sqmm.}</math></p> <hr/> <p>(24) Shear Force borne by Concrete  <math>t_{uc}</math>=permissible bond stress borne by concrete dependent on % age steel and grade of concrete          For <math>\leq 0.15\%, 0.25\%, 0.50\%</math> of steel          M15,<math>t_{uc} = 0.28, 0.36, 0.48 \text{ N/sq.mm}</math>          M20,<math>t_{uc} = 0.29, 0.36, 0.49</math>          M25, <math>t_{uc} = 0.29, 0.37, 0.50</math> respectively.</p> <hr/> <p>(25)Shear stress borne by concrete for slab  <math>= k \times t_{uc}</math>  <math>K</math>=coefficient dependent on slab thickness.          Slab depth=150mm or less,175mm,200mm, 225mm, 250mm, 275mm,300mm or more.  <math>K=1.3, 1.25, 1.20, 1.15, 1.10, 1.05, 1.00</math> respectively.</p> <hr/> <p>(26)Maximum Shear stress borne by concrete.  <math>t_{uc}</math> maximum = dependent on concrete grade.  <math>t_{uc}</math> maximum =2.5,2.8,3.1,3.5,3.7,4.0 for respectively concrete gradesM15,20,25,30,35,40.  <math>t_{uc}</math> maximum =3.25,3.5,3.72,4.025,4.07,4.20 for slab under concrete grade15,20,25,30,35,40.</p> <hr/> <p>(28)<math>t_{uv} &gt; t_{uc}</math> maximum =need to change the design.</p>
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<p>(B) <math>t_v = t_c/2</math> or <math>t_v = t_c</math>, Shear needed to adjust with stirrups with minimum spacing. <math>S = 0.87f_y.A_{sv}/0.4b</math>, Here <math>S</math>=spacing, <math>b</math>=width of beam.</p> <p>(C) <math>t_v &gt; t_c &lt; t_c</math> maximum for beam Or <math>t_v &gt; k \times t_c &lt; t_c</math> maximum Then <math>t_r = t_v - t_c</math> here <math>t_r</math>=remaining shear stress <math>V_r</math>=remaining shear force = <math>t_r \times b.d</math> <math>V_b</math>=shear force borne by bent-up bar = <math>0.707 \times A_{sv} \times s_v</math> for <math>\sin 45^\circ</math>, <math>A_{sv}</math>=area of bent-up bar, <math>V_s = V_b/2</math>=shear force borne by stirrups. Here <math>V_b &gt; V_r/2</math>, Spacing <math>S = A_{sv} \times s_v \times d / V_s</math> <math>S</math> should not be more than the lesser value of <math>0.75d</math> or <math>300\text{mm}</math>.</p> <hr/> <p>(30) Development length <math>L_{dt}</math>=development length in tension = bar dia. <math>\times</math> <math>s_t/4</math> <math>t_{bdt}</math> Here <math>t_{bdt}</math> = permissible bond stress in tension <math>s_t</math>=permissible tensile stress of steel. Value of <math>t_{bdt}</math>=0.6,0.8,0.9,1.0,1.1 for Fe-250 grade and respective grades of concrete like M-15,20,25,30,35 Value of <math>t_{bdt}</math>=0.96,1.28, 1.44, 1.60, 1.76 for Fe-415 or 500 grade with respective concrete grade like M-15,20,25,30,35.</p> <hr/> <p>(31) Development length of steel in compression = <math>L_{dc}</math> = bar dia. <math>\times</math> <math>s_t/5</math> <math>t_{bdt}</math></p> <hr/> <p>(32) Checking in development length <math>L_{dt} \leq 1.3 M_1 \div V + L_o</math> Here <math>M_1</math>=bending moment of straight bar at ends bottom, <math>V</math>=shear force, <math>L_o</math>= Anchorage length = <math>12 \times</math> bar dia or <math>d</math>, whichever is more.</p> <hr/> <p>(33) Design step for singly RCC beam (a) depth <math>d</math> assumed = span/10 to span /15 (b) <math>b = d/2</math> to <math>d/3</math> (c) Dead load of beam <math>W_d = b \times D \times 1 \times</math> density of rcc (d) Live Load <math>w_{live}</math> = Given (e) Total load <math>w = w_d + w_{live}</math>  (f) Effective length <math>l = L + B</math> or <math>L + d</math> whichever is less. (g) Maximum bending Moment <math>M = w.l.l/8</math> say (h) moment resisting factor <math>Q = 0.5.c.v.c.(X1).(Z1)</math> (i) <math>d</math> required = <math>M/Q.b</math> whole power 0.5 (j) compare <math>d</math> required &amp; <math>d</math> assumed <math>D</math> assumed <math>&gt;</math> or = <math>d</math> required it's ok If <math>d</math> assumed <math>&lt;</math> <math>d</math> required, then again design.  (k) <math>A_{st}</math> required = <math>M/s_t.z1.(d</math> required)</p>	<p>-----</p> <p>(29) Design for shear Reinforcement. (A) <math>t_u v &lt; t_u c/2</math> = No Shear (B) <math>t_u c &gt;</math> or = <math>t_u v</math> minimum shear Spacing <math>S_v = 0.87.f_y.A_{sv}/(0.4b)</math>  (C) <math>t_u v &gt; t_u c &lt; t_u c</math> maximum or <math>t_u v &gt; k.t_u c &lt; t_u c</math> maximum shear remaining = <math>t_u r = t_u v - t_u c</math> <math>V_{ur} = t_u r.b.d</math> <math>V_{ub} = 0.707.A_{sv}.s_v</math> <math>V_{us} = V_{ur}/2</math> and <math>V_{ub} &gt; V_{ur}/2</math> Spacing <math>S = 0.87f_y.A_{sv}.d/V_{us}</math> <math>0.75d</math> or <math>300\text{mm}</math> Overall whichever is less.</p> <hr/> <p>(30) Development Length <math>L_{dt}</math>=development length in tension = <math>0.87f_y.</math> bar diameter / <math>4t_{bdt}</math> <math>t_{bdt}</math> is dependent on bar size, surface roughness of bar, compaction and grade of concrete. <math>t_{bdt} = 1.2, 1.4, 1.5, 1.7, 1.9</math> for plain bars for respective concrete grades M20,25,30,35,40. Also <math>t_{bdt}</math> for deformed bars = <math>1.92, 2.24, 2.4, 2.72, 3.04</math> for respective grades of concrete.</p> <hr/> <p>(31) <math>L_{dc}</math> = development length of steel in compression = <math>0.87f_y.</math> bar diameter / <math>5 t_{bdt}</math>.</p> <hr/> <p>(32) Checking in development length <math>L_{dt} \leq M_1 \div V_u + L_o</math> <math>M_1 = A_{st} \times 0.87f_y \times Z</math> <math>A_{st}</math> = area of straight bar without bent-up bar.</p> <hr/> <p>(33) Design of Singly reinforced beam (a) Assumed <math>d</math> = span/10 to span /15 (b) <math>b = d/2</math> to <math>d/3</math> (c) Dead load of beam <math>W_d = b \times D \times 1 \times</math> density of rcc... (d) Live Load <math>w_{live}</math> = Given (e) Total load <math>w = w_d + w_{live}</math> <b>Factored load <math>w_u = 1.5(w_d + w_{live})</math></b> (f) Effective length <math>l = L + B</math> or <math>L + d</math> whichever is less. (g) Maximum Bending Moment <math>M = w_u.l.l/8</math> (h) <math>Q_u = 0.36f_{ck}.X_{u\max}(1 - 0.42X_{u\max}/d)/d</math> (i) <math>d</math> required = <math>(M_u/Q_u.b)</math> whole power 0.5 (j) compare <math>d</math> required &amp; <math>d</math> assumed Condition:- <math>D</math> assumed <math>&gt;</math> or = <math>d</math> required it's ok If <math>d</math> assumed <math>&lt;</math> <math>d</math> required, then again design. If under reinforced means <math>d</math> assumed <math>&gt;</math> <math>d</math> required <math>M_u = 0.87f_y.A_{st}.d[1 - A_{st}.f_y/b.d.f_{ck}]</math></p>
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<p>(l) <math>A_{st \text{ min.}} = 0.85 \text{ bd/fy}</math></p> <p>(m) <math>A_{st \text{ max.}} = 0.04 \text{ b.D}</math></p> <p>(n) <math>A_{st \text{ required}} &gt; A_{st \text{ min.}}</math>, <math>A_{st \text{ required}} &lt; A_{st \text{ max.}}</math></p> <p>(o) <math>N = \text{number of bars} = A_{st}/ast</math></p> <p><math>A_{st \text{ actual}} = (N)(ast)</math></p> <p>(p) Decide number of bent-up bars.</p> <p>(q) Check the beam in Shear and Bond, <b>not in deflection</b></p> <p><b>IN SHEAR</b>  <math>t_v &gt; t_c &lt; t_c \text{ maximum for beam}</math>      Or  <math>t_v &gt; k \times t_c &lt; t_c \text{ maximum}</math>      Then <math>t_r = t_v - t_c</math> here <math>t_r = \text{remaining shear stress}</math>  <math>V_r = \text{remaining shear force} = t_r \times b.d</math>  <math>V_b = \text{shear force borne by bent-up bar} = 0.707 \times A_{sv} \times s_v</math> for  <math>\sin 45^\circ</math>, <math>A_{sv} = \text{area of bent-up bar}</math>, <math>V_s = V_b/2 = \text{shear force}</math>      borne by stirrups.      Here <math>V_b &gt; V_r/2</math>, Spacing <math>S = A_{sv} \times s_v \times d / V_s</math>  <math>S</math> should not be more than the lesser value of <math>0.75d</math> or  <math>300\text{mm}</math>.</p> <p>-----</p> <p><b>IN BOND</b>      Development length  <math>L_{dt} = \text{development length in tension}</math>  <math>= \text{bar dia.} \times s_t / 4 t_{bdt}</math>      Here <math>t_{bdt} = \text{permissible bond stress in tension}</math>  <math>s_t = \text{permissible tensile stress of steel}</math>.      Value of <math>t_{bdt} = 0.6, 0.8, 0.9, 1.0, 1.1</math> for Fe-250 grade and      respective grades of concrete like M-15,20,25,30,35      Value of <math>t_{bdt} = 0.96, 1.28, 1.44, 1.60, 1.76</math> for Fe-415 or      500 grade with respective concrete grade like      M-15,20,25,30,35.</p> <p>-----</p> <p>Development length of steel in compression  <math>= L_{dc} = \text{bar dia.} \times s_t / 5 t_{bdt}</math></p> <p>-----</p> <p>development length  <math>L_{dt} \leq 1.3 M_1 / V + L_o</math>      Here <math>M_1 = \text{bending moment of straight bar at ends bottom}</math>,  <math>V = \text{shear force}</math>, <math>L_o = \text{Anchorage length} = 12 \times \text{bar dia or } d</math>,      whichever is more.  <math>A_{st} = \text{area of straight bar without bent-up bar}</math>.</p> <p>-----</p>	<p>(k) Get <math>A_{st}</math> required  <math>\text{No of bars required} = A_{st}/ast \text{ round off.}</math>      For balance means <math>d = d</math> required  <math>\mu = A_{st} \times 0.87 f_y (d - 0.42 X_{u \text{ max}})</math></p> <p>(l) <math>A_{st \text{ min.}} = 0.85 \text{ bd/fy}</math></p> <p>(m) <math>A_{st \text{ max.}} = 0.04 \text{ b.D}</math></p> <p>(n) <math>A_{st \text{ required}} &gt; A_{st \text{ min.}}</math>, <math>A_{st \text{ required}} &lt; A_{st \text{ max.}}</math></p> <p>(o) <math>N = \text{number of bars} = A_{st}/ast</math></p> <p><math>A_{st \text{ actual}} = (N)(ast)</math></p> <p>(p) Decide number of bent-up bars.</p> <p>(q) Check in shear, bond and <b>deflection</b></p> <p><b>IN SHEAR</b>  <math>t_v &lt; t_c / 2 = \text{No Shear}</math>  <math>t_v &gt; \text{or} = t_v \text{ minimum shear}</math>      Spacing <math>S_v = 0.87.f_y.A_{sv} / (0.4b)</math>  <math>t_v &gt; t_c &lt; t_c \text{ maximum}</math>      or  <math>t_v &gt; k.t_c &lt; t_c \text{ maximum}</math>  <math>\text{shear remaining} = t_r = t_v - t_c</math>  <math>V_{ur} = t_r.b.d</math>  <math>V_{ub} = 0.707.A_{sv}.s_v</math>  <math>V_{us} = V_{ur}/2</math> and <math>V_{ub} &gt; V_{ur}/2</math>      Spacing <math>S = 0.87 f_y.A_{sv}.d / V_{us}</math>  <math>0.75d</math> or <math>300\text{mm}</math>      Overall whichever is less.</p> <p>-----</p> <p><b>IN BOND</b>      Development Length  <math>L_{dt} = \text{development length in tension}</math>  <math>= 0.87 f_y . \text{bar diameter} / 4 t_{bdt}</math>  <math>t_{bdt}</math> is dependent on bar size, surface roughness of bar,      compaction and grade of concrete.  <math>t_{bdt} = 1.2, 1.4, 1.5, 1.7, 1.9</math> for plain bars for respective      concrete grades M20,25,30,35,40.      Also <math>t_{bdt}</math> for deformed bars = 1.92, 2.24, 2.4, 2.72, 3.04      for respective grades of concrete.</p> <p>-----</p> <p><math>L_{dc} = \text{development length of steel in compression}</math>  <math>= 0.87 f_y . \text{bar diameter} / 5 t_{bdt}</math>.</p> <p>-----</p> <p>development length</p>
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<p>NO CHECK IN DEFLECTION</p> <p>-----</p> <p>(34) Doubly Rcc beam (a) Critical Neutral Axis <math>X_c = (m \cdot cbc \cdot d) / (m \cdot cbc + st)</math></p> <p>-----</p> <p>(b) Actual Neutral Axis <b>Xa</b></p> <p><math>b \cdot X_a \cdot X_a / 2 + (1.5m - 1) Asc (X_a - d') = m \cdot Ast (d - X_a)</math></p> <p>-----</p> <p>(c) Lever Arm for singly or due to concrete <math>Z' = (d - X_c / 3)</math> Lever Arm due to Asc <math>Z'' = (d - d')</math></p> <p>-----</p> <p>(d) Compressive Force due to singly <math>C' = b \times X_c \times cbc / 2</math> Compressive Force due to Asc <math>C'' = (1.5m - 1) Asc \times cbc'</math> Here <math>cbc' =</math> stress on the surface of Asc. <math>cbc' = cbc (X_c - d') / X_c</math></p> <p>-----</p> <p>(e) Bending Moment <math>M' =</math> bending moment due to singly <math>= C' \times Z'</math> <math>= b \times X_c \times cbc (d - X_c / 3) / 2</math> <math>M'' =</math> Bending Moment due to Asc <math>(1.5m - 1) Asc \times cbc' (d - d')</math></p> <p>-----</p> <p>(f) Stress of Steel in Compression <math>sc = 130, 130, 190, 190 \text{ N/square mm for}</math> Fe-250, 350, 415, 500. Asc = 10 square mm Equivalent area of concrete in compression <math>= (1.5 \times 18 - 1) \times 10 = 260 \text{ square mm.}</math></p> <p>-----</p> <p>(g) Determination of Moment Given data b, d, Asc, Ast, d'. <math>X_c = m \cdot cbc \cdot d / (m \cdot cbc + st)</math> Get Xa from equation <math>b \cdot X_a \cdot X_a / 2 + (1.5m - 1) Asc (X_a - d') = m \cdot Ast (d - X_a)</math> <b>Condition:- If <math>X_a &gt; X_c =</math> over reinforced</b> Concrete Will fail, hence moment <math>M_c = b \cdot X_a \cdot cbc (d - X_a / 3) / 2 + (1.5m - 1) Asc \cdot cbc' (d - d')</math></p> <p>If <math>X_a = X_c =</math> balance section <math>M_c = b \cdot X_a \cdot cbc (d - X_a / 3) / 2 + (1.5m - 1) Asc \cdot cbc' (d - d')</math></p>	<p><math>Ldt \leq M1 \div Vu + Lo</math> <math>M1 = Ast \times 0.87fy \times Z</math> Ast = area of straight bar without bent-up bar.</p> <p>-----</p> <p>CHECKING IN DEFLECTION service stress <math>fs = 0.58 \cdot fy (Ast \text{ required} / Ast \text{ provided})</math> From graph get modification factor k (l/d) maximum = 20.k for simply supported beam (l/d) maximum = 7k for cantilever beam (l/d) actual &lt; [(l/d) maximum]</p> <hr/> <p>(34) Doubly Rcc beam (a) Critical Neutral Axis <math>X_{umax} = 700d / (1100 + 0.87fy)</math></p> <p>-----</p> <p>(b) Actual Neutral Axis <b>Xu</b> Total compressive force C <math>C = C' + C'' =</math> compressive force due to compression zone concrete + Compressive force due to Asc <math>C' = 0.36fck \cdot Xu \cdot b</math> <math>C'' = fsc \cdot Asc - fcc \cdot Asc</math> <math>C = 0.36fck \cdot Xu \cdot b + Asc (fsc - fcc)</math> Tensile force = <math>T = 0.87fy \cdot Ast</math> <math>C = T</math> So <math>Xu = (0.87fy \cdot Ast - Asc \cdot fsc) / (0.36fck \cdot b)</math> Neglecting fcc</p> <hr/> <p>(c) Lever Arm For <math>Z' = L.A. = (d - 0.42x_{umax})</math> For <math>Z'' = L.A. = (d - d')</math></p> <p>-----</p> <p>(c) Compressive Force <math>C = 0.36 \cdot fck \cdot X_{umax} \cdot b + Asc \cdot fsc</math></p> <p>-----</p> <p>(e) Bending Moment <math>M = M' + M''</math> <math>M' = C' \times Z' = 0.36 \cdot fck \cdot X_{umax} \cdot b (d - 0.42x_{umax})</math> <math>M'' = C'' \times Z'' = fsc \cdot Asc (d - d')</math></p> <p>-----</p> <p>(f) Stress of steel in compression fsc Dependent on d'/d <math>fsc = 217, 217, 217, 217</math> for Fe-250, respectively d'/d for 0.05, 0.10, 0.15, 0.20. <math>fsc = 355, 353, 342, 329</math> for Fe-415. <math>fsc = 424, 412, 395, 370</math> for Fe-500. <math>fsc = 458, 441, 419, 380</math> for Fe-550.</p> <p>-----</p> <p>(g) Determination of Moment Given data b, d, Asc, Ast, d'. <math>Xu = (0.87fy \cdot Ast - fsc \cdot Asc) / (0.36fck \cdot b)</math> fsc can be from d'/d from table <math>X_{umax} = 700d / (1100 + 0.87fy)</math> Condition</p>
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<p>If <math>X_a &lt; X_c</math> = under reinforced Steel will fail. Now transfer the st to cbc' at top of beam on compression zone. Also at Asc get the value of cbc" <math>b.X_a.cbc'(d-X_a/3) + (1.5m-1)Asc.cbc''(d-d')</math></p> <p>-----</p> <p><b>(i) Finding Asc and Ast</b>  <math>X_c = (m.cbc.d/m.cbc+st)</math>  <math>cbc' = cbc(X_c - d')/X_c</math>  <math>M_1 = \text{Moment due to singly} = b.X_c.cbc(d-X_c/3)/2</math>  <math>M_2 = M - M_1 = \text{Moment due to Asc}</math>  <math>M_2 = (1.5m-1)Asc.cbc'(d-d')</math>  Asc can be had from above.  Ast1 = steel required for singly.  <math>Ast_1 = M_1/st(d-X_c/3)</math>  Ast2 = area of steel in tension due to Asc  <math>Ast_2 = M_2/sc(d-d')</math>  <b>Ast = Ast1 + Ast2 = total steel in tension.</b></p> <p>-----</p> <p><b>(35) Tee Beam Design</b>  (a) Depth of T beam  <math>d = \text{effective depth} = \text{span}/10 \text{ to } \text{span}/15,</math>  <math>bw = \text{width of beam} = d/3 \text{ to } 2d/3</math>  (b) <math>bf = \text{width of flange} = lo \div 6 + bw + 6Df</math>  Or  <math>bf = bw + A/2 + B/2</math>  (c) NEUTRAL AXIS  Critical Neutral Axis <math>X_c = (m.cbc.d/m.cbc+st)</math>  Actual Neutral Axis <math>X_a</math>, when <math>X_a &lt; Df</math> or <math>X_a = Df</math>  <math>bf.X_a.X_a/2 = m.Ast.(d-X_a)</math>  If <math>X_a &gt; Df</math>, then  <math>bf.Df(X_a - Df/2) + bw(X_a - Df)(X_a - Df)/2 = m.Ast(d - X_a)</math>  Get <math>X_a</math>.  If <math>X_a &lt; X_c</math> = under reinforced  <math>X_a = X_c</math> = balance  <math>X_a &gt; X_c</math> = over reinforced  (g) Lever Arm  <math>X_a &lt; Df</math> Lever Arm = <math>d - X_a/3</math>  <math>X_a = Df</math> Lever Arm = <math>d - Df/3</math>  <math>X_a &gt; Df</math> <math>Z' = d - y</math> <math>Z'' = [d - (Df + (X_a - Df)/3)]</math>  (h) <b>Compressive Force C</b>  When <math>X_a &lt; Df</math> <math>C = bf.X_a.cbc(d - X_a/3)/2</math>  When <math>X_a = Df</math> <math>C = bf.Df.cbc(d - Df/3)/2</math>  When <math>X_a &gt; Df</math> <math>C = C' + C''</math>  <math>C' = bf.Df(cbc + cbc')(d - y')/2</math>  <math>y' = (2.cbc + cbc')(Df/3)/(cbc + cbc')</math>  <math>C'' = (bw)(X_a - Df)(cbc'/2)(Z'')</math>  <math>Z'' = d - [Df + (X_a - Df)/3]</math></p> <p>-----</p> <p><b>(36) Column design</b>  (a) Effective Length l  <math>l = 0.65 L</math> for both end fixed  <math>l = 0.80L</math> when one end fixed and another end free.  (b) Short Column  <math>l/b \leq 12</math>  Long Column  <math>l/b &gt; 12</math></p>	<p><math>X_u &gt; X_{u\max}</math> = over reinforced  <math>\mu</math> is calculated by <math>X_{u\max} = X_u</math></p> <p>If <math>X_u = X_{u\max}</math>  <math>\mu = 0.36f_{ck}.X_{u\max}.b</math>  <math>(d - 0.42X_{u\max}) + Asc.(f_{sc} - f_{cc})(d - d')</math>  If <math>X_u &lt; X_{u\max}</math>  <math>\mu = 0.36f_{ck}.X_u(b)(d - 0.42X_u) + Asc(f_{sc} - f_{cc})(d - d')</math></p> <p>-----</p> <p><b>(i) Finding Asc and Ast</b>  <b>Ast' = <math>\mu_{limit} / (0.87 f_y (d - 0.42 X_{u\max})</math></b>  <b><math>\mu'' = \mu - \mu_{limit}</math></b>  <b>Ast'' = <math>\mu'' / (0.87.f_y)(d - d')</math></b>  <b>Ast = Ast' + Ast''</b>  <b>Asc = <math>\mu'' / f_{sc} (d - d')</math></b></p> <p>-----</p> <p><b>(35) Tee Beam LSM</b>  (a) Depth of T beam  <math>d = \text{Span}/10 \text{ to } \text{Span}/15</math>  Breadth of beam <math>bw = d/3 \text{ to } 2d/3</math>  (b) Width of flange = <math>bf = lo \div 6 + bw + 6Df</math>  Or  <math>bf = bw + A/2 + B/2</math>  (3) NEUTRAL AXIS  Critical Neutral Axis = <math>X_{u\max} = 700d / (1100 + 0.87f_y)</math>  Actual Neutral Axis <math>X_u</math>, when <math>X_u &lt; Df</math> or <math>X_u = Df</math>  <math>X_u = 0.87.f_y.Ast / 0.36.f_{ck}.bf</math>  If <math>X_u &gt; Df</math>, Also <math>X_u = X_{u\max}</math> and <math>Df &lt; 3.X_u/7</math> or <math>Df = 3X_u/7</math>, then stress block will lie rectangular and remaining parabolic.  If <math>Df &gt; 3.X_u/7</math>, then stress block will lie rectangular upto <math>3X_u/7</math> and rest parabolic.  If <math>X_{u\max} = X_u, X_u &gt; Df</math> and <math>Df/d \leq 0.2</math> or <math>Df &lt; 3X_u/7</math>  <math>C_u = 0.36.f_{ck}.bw.X_{u\max} + 0.446f_{ck}(bf - bw).Df</math>  Total tension <math>T_u = 0.87 f_y.Ast</math>  IF <math>X_{u\max} = X_u, X_u &gt; Df</math> and <math>Df/d &gt; 0.2</math>  <math>C_u = 0.36.(X_{u\max}/d)f_{ck}.bw.d + 0.45 f_{ck}(bf - bw).Y_f</math>  Here <math>Y_f = 0.15 X_u + 0.65 Df</math>  <math>X_{u\max} &gt; X_u, X_u &gt; Df, Df &lt; 3X_u/7</math>  <math>C_u = 0.36f_{ck}.bw.X_u + 0.446 f_{ck}(bf - bw).Df</math>  <math>T_u = 0.87f_y.Ast</math>  <math>X_{u\max} &gt; X_u &gt; Df, Df &gt; 3X_u/7</math>  <math>C_u = 0.36f_{ck}.bw.X_u + 0.45f_{ck}.Y_f(bf - bw)</math>  Here <math>Y_f = 0.15X_u + 0.65.Df</math>, <math>Y_f &lt; Df</math> or <math>Y_f = Df</math>  <math>X_u &gt; X_{u\max}</math> means over reinforced  Redesign</p> <p>-----</p> <p><b>(36) Column design</b>  (a) Effective Length l  <math>l = 0.65 L</math> for both end fixed</p>
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<p>Column Axial Load <math>P=A_c.c_c+A_s.c_s</math>  (c) Longitudinal bar dia=12 mm to 50 mm.  Lateral ties bar dia=8mm to 12 mm or bar dia/4, whichever is maximum.  (d) Independent ties spacing  Least dimension of column  or  <math>16 \times \text{bar diameter}</math> or  or  300mm whichever is less.  (e) Spiral reinforcement  Pitch max=75 mm or Core diameter/6 whichever is minimum  Pitch minimum =25 mm or <math>3 \times \text{ties dia}</math>  Whichever is less.</p> <p>-----</p> <p>(f) cbc and cc value  M15-cbc=5, cc=4, M20-cbc=7, cc=5,  M25-cbc=8.5, cc=6, M30-cbc=10, cc=8,  Fe-250-st=140, sc=130, Fe-350-st=190, sc=190,  Fe-415-st=230, sc=190, Fe-275-st=275, sc=190 N/square mm.</p> <p>-----</p> <p>(g) Strength for short Column for non helical  <math>P=A_k.c_c+A_s.c_s</math>  <math>A_g</math>=gross area of column =<math>3.14 \times d \times d/4</math>  <math>D_k</math>=Core diameter  =<math>D-2 \times \text{cover}+2 \times \text{ties diameter}</math>  <math>A_k</math>=Core Area=(<math>3.14 \times D_k \times D_k/4</math>)-<math>A_s.c_s</math>  <math>V_u</math>=volume of spiral for per pitch height.</p>	<p><math>l=0.80L</math> when one end fixed and another end free.  (b) Short Column  <math>e_{\text{min}}=l/500 +D/30 &gt; \text{or} =20 \text{ mm}</math>  <math>e_{\text{min}}</math> should not be greater than <math>0.05D</math></p> <p>Column factored load <math>P_u=0.4f_{ck}.A_c+0.67f_y.A_s</math>  (c) Longitudinal bar dia=12 mm to 50 mm.  Lateral ties bar dia=8mm to 12 mm or bar dia/4, whichever is maximum.  (d) Independent ties spacing  Least dimension of column  or  <math>16 \times \text{bar diameter}</math> or  or  300mm whichever is less.  (e) Spiral reinforcement  Pitch max=75 mm or Core diameter/6 whichever is minimum  Pitch minimum =25 mm or <math>3 \times \text{ties dia}</math>  Whichever is less.</p> <p>-----</p> <p>(f)  NO NEED</p> <p>-----</p> <p>(g) Strength for short Column for non helical  Factored load <math>P_u=0.4f_{ck}.A_c+0.67f_y.A_s</math></p>
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### CONCLUSION

The title demonstrates the pros and cons, while differentiating the WSM to LSM method of designing of RCC structures. In existing scenario LSM method is in vogue and while designing, the incoming load is multiplied by load factor 1.5 and also the permissible stresses are more in steel and concrete in bending and in compression too. Even this act, the section in LSM remains small and steel used remains more than WSM, even this, the valuation remains economical for LSM. Though steel is costlier than concrete by 70 times, even than designing of RCC sections through LSM are cheaper. The technical paper is covering maximum differentiation as seemed sufficient and enough for learning purpose. Effective points will enhance the readers knowledge.

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