



# Approximating fixed points of nearly asymptotically nonexpansive mappings in $CAT(k)$ spaces

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**Abstract.** In this paper we approximate common fixed points of nearly asymptotically nonexpansive mappings under modified  $SP$ -iteration process in the setting of  $CAT(k)$  spaces and establish strong and  $\Delta$ -convergence theorems. Our results generalize and improve the corresponding known results of the existing literature.

**Keywords:**  $\Delta$ -convergence; Modified  $SP$ -iteration process; Nearly asymptotically nonexpansive mapping; Common fixed point;  $CAT(k)$  space

**Mathematics Subject Classification:** 47H09; 47H10

## 1. INTRODUCTION

The class of asymptotically nonexpansive mappings was introduced by Goebel and Kirk [8] as an important generalization of the class of nonexpansive mappings. They proved that if  $K$  is a nonempty closed and bounded subset of a uniformly convex Banach space, then every asymptotically nonexpansive self-mapping of  $K$  has a fixed point. There are many papers dealing with the approximation of fixed points of asymptotically nonexpansive mappings and asymptotically quasi-nonexpansive mappings in uniformly convex Banach spaces, using modified Mann, Ishikawa and three-step iteration processes (see, [8, 16, 23, 24, 26, 27, 29–34]).

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